

QUANTUM ENGINEERING

# Optimization of Heat Exchanger Design with Zig-Zag Flow: Minimum Volume Design Satisfying Structural and Thermal Requirements



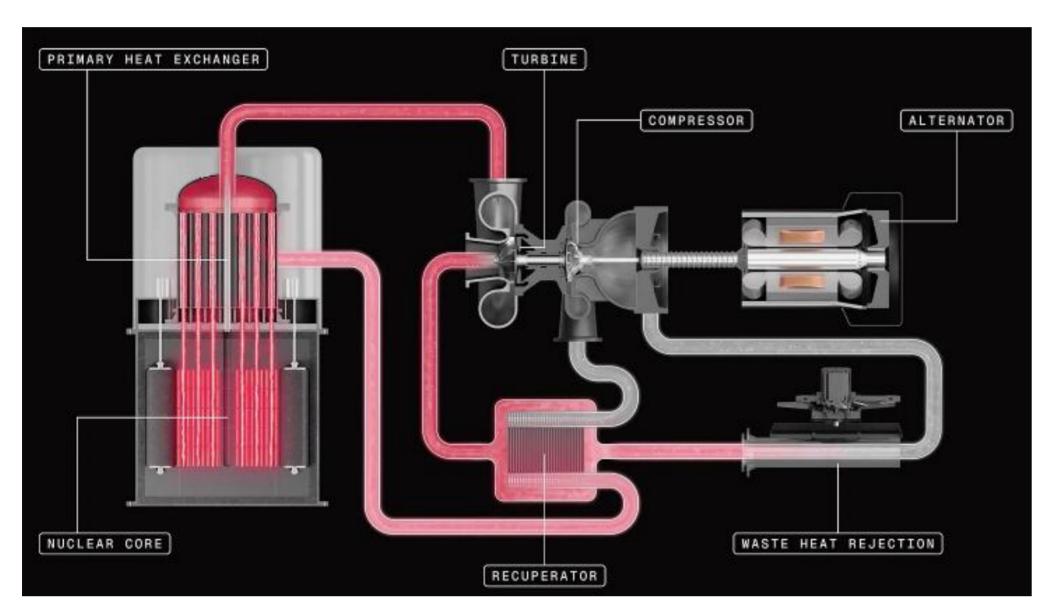
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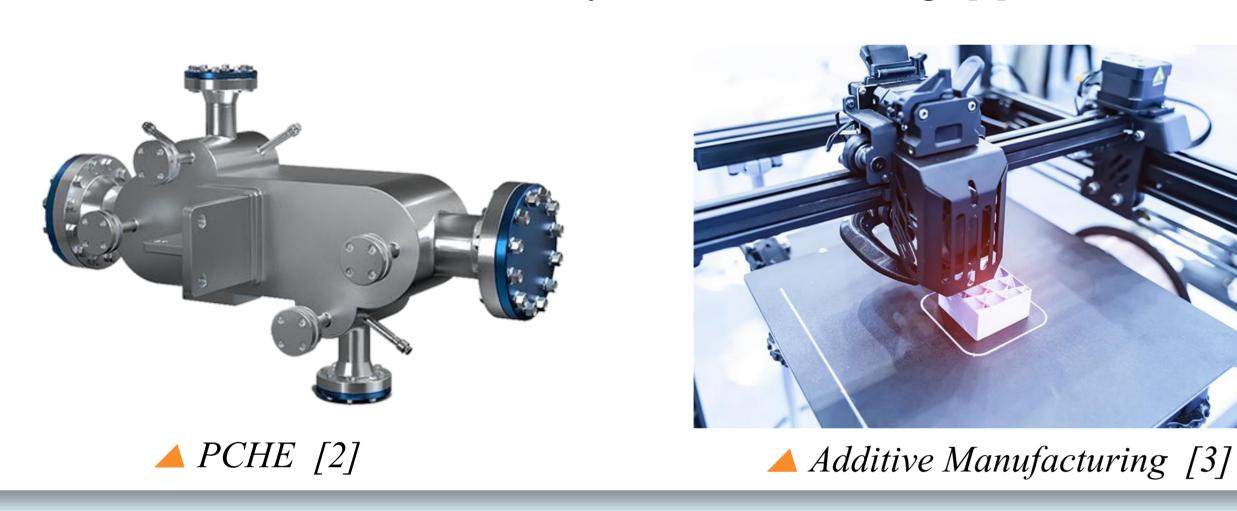
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## Introduction

- Zig-zag channels are key for SMRs and supercritical CO<sub>2</sub> (s-CO<sub>2</sub>) Brayton cycles, enabling high heat transfer in compact, high-pressure hardware.
- Printed Circuit Heat Exchangers (PCHEs) which are made by diffusion-bonding etched plates offer high heat-transfer coefficients, exceptional pressure tolerance, and compactness, suiting nuclear and power-cycle service.
- Conventional photochemical etching caps channel diameters at ~2.5 mm; this work evaluates 3–4 mm s-CO<sub>2</sub> channels for heat-transfer efficiency, pressure drop, and structural integrity.
- Additive manufacturing, while outside the strict PCHE definition, is explored as a route to PCHE-like geometries with greater design freedom.



▲ Schematic of Nuclear reactor design [1]

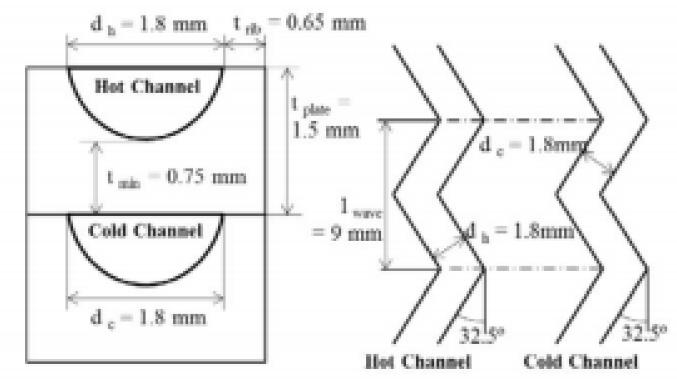


### Methodology

■ The optimization assumed a recuperator with fixed boundaries, using s-CO₂ on both hot and cold sides and prescribing mass flow rates, inlet/outlet temperatures, and pressures

| Parameter                      | Value             |  |  |  |  |
|--------------------------------|-------------------|--|--|--|--|
| Hot-side inlet temperature     | 730 K             |  |  |  |  |
| Cold-side inlet temperature    | 500 K             |  |  |  |  |
| Hot side inlet pressure        | 9 MPa             |  |  |  |  |
| Cold side inlet pressure       | 22.5 MPa          |  |  |  |  |
| Working fluid                  | S-CO <sub>2</sub> |  |  |  |  |
| Hot side total mass flow rate  | 80  kg/s          |  |  |  |  |
| Cold side total mass flow rate | 100 kg/s          |  |  |  |  |

▲ Baseline Operating Conditions for PCHE design



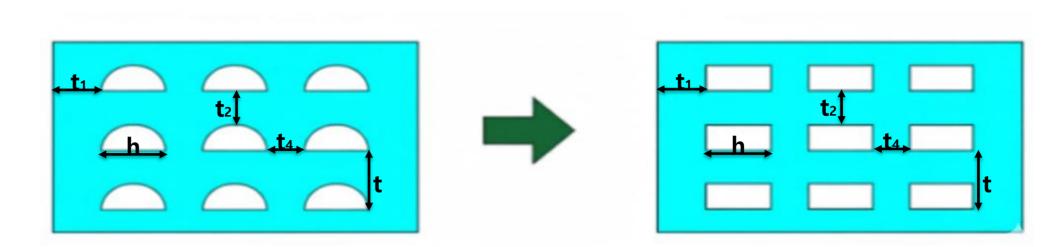
▲ Channel Geometry of 1.8mm diameter PCHE

Channel diameters were scaled from the ~1.8 mm etched baseline to 3–4 mm as PCHE-like geometries to test thermal performance and compliance with specifications, including pressuredrop limits.

Structural feasibility was checked against ASME BPVC Section VIII, Division1, Appendix13. Thermal-hydraulic behavior in zig-zag channels was simulated with the KAIST HXD MATLAB code to predict s-CO<sub>2</sub> heat transfer and pressure loss.

### Results

The 1.8 mm design is the most compact but suffers from high pressure drops, the 3.0 mm design offers the best balance of thermal performance and pressure drop, while the 4.0 mm design, though structurally feasible, results in a larger volume and reduced thermal performance.



| Parameter      | Description                                  |  |  |  |  |  |
|----------------|--|--|--|--|--|--|
| <b>t</b> 1     | Side wall thickness                          |  |  |  |  |  |
| t <sub>2</sub> | Channel-to-channel vertical wall thickness   |  |  |  |  |  |
| t4             | Overall plate thickness                      |  |  |  |  |  |
| t              | Channel-to-channel horizontal wall thickness |  |  |  |  |  |
| h              | h Channel diameter                           |  |  |  |  |  |

PCHE Geometry and Dimensional Parameters

| Channel diameter (mm) | N_<br>Channel | L<br>(m) | Optimal<br>(a*b) | width<br>(m) | Thick ness (m) | Volume<br>(m 3) | Inlet T (K) / P (MPa) | ΔP_hot / ΔP_col d (kPa) | Heat duty (MW <sub>th</sub> ) | Peak stress ≤<br>allow<br>(MPa) |
|-----------------------|---------------|----------|------------------|--------------|----------------|-----------------|-----------------------|-------------------------|-------------------------------|---------------------------------|
| 1.8                   | 92,000        | 0.60     | 125*736          | 0.230        | 1.254          | 0.173           | 730 / 9               | 199.32 /<br>109.12      | 20.06                         | σstay : 88.387<br>≤ 89.997      |
| 3.0                   | 33,000        | 1.08     | 132*250          | 0.406        | 0.694          | 0.304           | 730 / 9               | 195.42 /<br>106.96      | 20.04                         | $\sigma long: 89.99 \le 89.998$ |
| 4.0                   | 18,400        | 1.52     | 115*160          | 0.750        | 0.407          | 0.465           | 730 / 9               | 198.36 /<br>108.32      | 19.96                         | σstay : 88.247 $≤ 93.007$       |

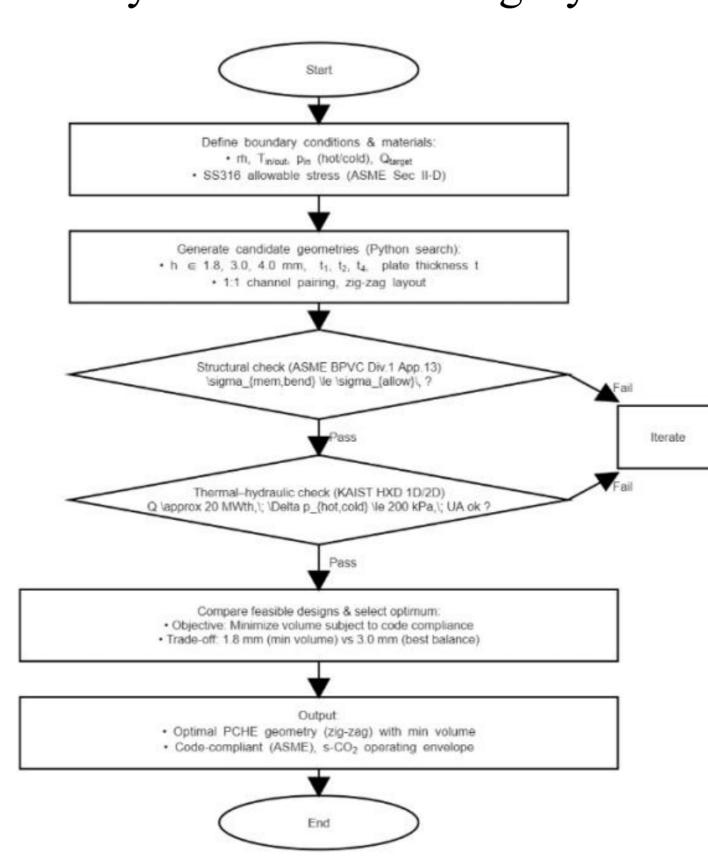
Optimal partitions, dimensions and performance indicators

## Discussion

- Minimizing volume is a trade-off: longer channels add area but raise  $\Delta p$  (Darcy–Weisbach), and too much  $\Delta p$  can push CO<sub>2</sub> out of the supercritical regime—so strict pressure-drop limits are required.
- Structural limits are set mainly by external-pressure buckling of wide plates; smaller diameters help heat transfer but risk fouling and face etching/bonding limits. SS316 is corrosion-resistant at high T, yet allowable stress falls with temperature, so conservative margins are needed.
- KAIST HXD 1D/2D modeling captures zig-zag effects beyond simple correlations, enabling a balanced feasibility check of 3–4 mm channels for both thermal-hydraulic performance and structural integrity.

#### Conclusion

■ A zig-zag PCHE design workflow was established to minimize volume while satisfying thermal-hydraulic and structural requirements, including geometry selection and integrity checks.



Extending beyond ~2.5 mm to 3–4 mm channels clarifies key sCO<sub>2</sub> trade-offs and informs future heat-exchanger development.

The 1.8 mm channel is most

compact but incurs excessive

pressure drop; the 3.0 mm channel

offers the best performance— $\Delta p$ 

trade-off and is most practical; the

but

structurally

thermally

4.0 mm channel is

inefficient and larger.

acceptable

▲ PCHE Zig-Zag Design Procedure (Minimum Volume under Structural and Thermal Constraints)

- [1] Antares Industries. Official website.
- [2] SHENSHI EC. PCHE (Printed Circuit Heat Exchanger)
- [3] Manufacturing Digital. Next-level 3D printing developed by the University of Tokyo
- [4] Baik, S., Kim, S. G., Son, S., Kim, H. T., & Lee, J. I. (2015). Printed circuit heat exchanger design, analysis and experiment. In NURETH-16, Chicago, IL: ANS