

## Experimental approach to measure windage loss in supercritical CO<sub>2</sub> condition

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### 1. Introduction

A concept of fully modularized fast reactor with a supercritical CO<sub>2</sub> (S-CO<sub>2</sub>) cooled direct Brayton cycle, namely KAIST Micro Modular Reactor (MMR), for 10MWe power output is developed for the distributed power generation using the nuclear energy. The supercritical CO<sub>2</sub> (S-CO<sub>2</sub>) Brayton cycle has high performance in power conversion. It has high efficiency at moderate temperature range, high compactness and simple configuration[1]. This is because S-CO<sub>2</sub> has nonlinear property change without phase change near the critical point(7.38MPa, 31°C)[2]. However, this nonlinearity makes the control of this system difficult. Furthermore, due to the high density of S-CO<sub>2</sub>, the windage loss becomes significant in the rotating machinery [3]. Dramatic property change of CO<sub>2</sub> near critical point becomes a challenge to develop a good windage loss model for S-CO<sub>2</sub> conditions. In this paper, the windage loss model of the S-CO<sub>2</sub> turbomachinery is investigated. In addition, measuring windage loss will be performed at the Autonomous Brayton Cycle loop (ABC loop) constructed in KAIST. The loop is designed to investigate the S-CO<sub>2</sub> Brayton cycle's performance and develop design methods of the components.

### 2. Windage loss in S-CO<sub>2</sub> Brayton Cycle

#### 2.1 S-CO<sub>2</sub> Brayton Cycle

S-CO<sub>2</sub> has nonlinear property changes near the critical point as shown in Fig 1. These characteristics make the S-CO<sub>2</sub> Brayton cycle to have advantages of both gas Brayton cycles and steam Rankine cycles. It has compact turbomachinery and simple configuration because of no phase change. In addition, it achieves reduced compression work and high efficiency. Fig 2 shows CO<sub>2</sub>'s low compressibility when it is in supercritical state. Fig 3 [4] shows efficiency of various power cycles.

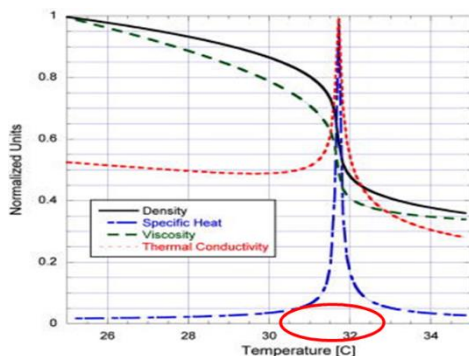


Fig 1. Nonlinear thermo-physical properties of CO<sub>2</sub> near critical point (7.4 MPa)

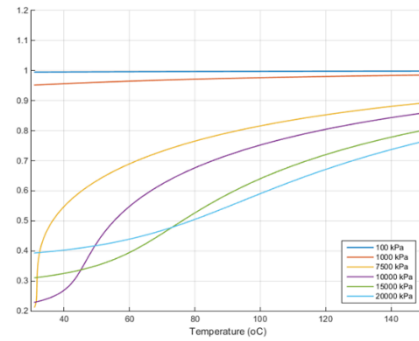


Fig 2. Compressibility factor of CO<sub>2</sub>

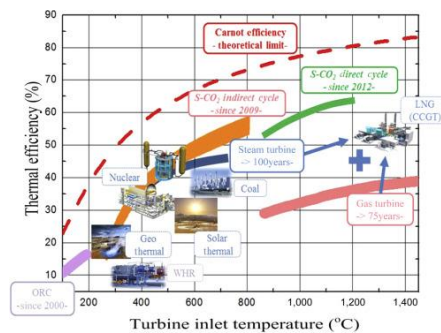


Fig 3. Efficiency of various power cycles

However, despite of these advantages, S-CO<sub>2</sub> Brayton cycle has technical challenges originating from dramatic property changes of CO<sub>2</sub> near the critical point. This characteristics of CO<sub>2</sub> affect the controllability of the system. In addition, the component should be able to handle the unexpected instability.

#### 2.2 Windage loss in S-CO<sub>2</sub> Brayton Cycle

There are several losses while operating turbomachinery. The internal loss is caused in the main flow path while the external loss in the minor flow paths. The internal losses hinder the performance of compressor and the external losses increase input work of the turbomachinery. From the previous experiments, the external losses can be substantial [5].

The windage loss (shaft friction loss) is one of the external losses which is generated by secondary flow. The secondary flow is a rotational flow induced by the rotating shaft's surface. The viscous skin friction acts as torque on the shaft and therefore additional power is needed to overcome this resistance. This loss is not only a function of the turbomachinery geometry but also the fluid's property. The main variables are the shaft length, clearance between the shaft and the wall (stator), density and viscosity of the fluid.

As presented in reference [3], in an S-CO<sub>2</sub> system, the windage loss is a major cause of power loss so the minimization of the loss is necessary to commercialize the S-CO<sub>2</sub> system. However, in the case of S-CO<sub>2</sub> turbomachinery, there are only studies of total external losses. Therefore, the windage loss models are reviewed in this study. Windage loss models were developed in the previous studies [6, 7]. Those models are shown in the equations below.

Mack's model

$$C_f = \begin{cases} \frac{1.8}{Re c_r^{1/4}} \frac{(1 + c_r)^2}{(1 + c_r)^2 - 1}, & Ta \leq 41.3 \text{ (laminar flow)} \\ \frac{K}{Ta^{1/5}}, & Ta > 400 \text{ (fully turbulent flow)} \end{cases}$$

Modified Mack's model

$$C_f = \begin{cases} \frac{4}{Re} \frac{(1 + c_r)^2}{(1 + c_r)^2 - 1}, & Ta \leq Ta_{crit} \\ \frac{K}{Ta^{1/5}}, & Ta > Ta_{crit} \end{cases}$$

Vrancik's model

$$C_f = \begin{cases} \frac{2}{Re}, & \text{(laminar flow)} \\ \frac{1}{\sqrt{C_f}} = B + 1.768 \ln(Re \sqrt{C_f}), & \text{(turbulent flow)} \end{cases}$$

These models are used to calculate the windage loss from the experimental shaft trajectory data as shown in Figs. 4 to 6. The viscosity and density around the shaft are calculated from the previous study [8]. For the early stage of the research, the calculation is simplified by assuming that properties are uniform in axial direction. The time step is 0.0001 sec. The clearance is 200  $\mu$ m and the axial length is 200 mm. inlet conditions of each test is shown in Fig. 7.

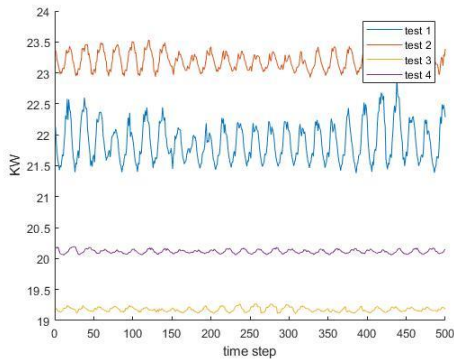


Fig 4. Windage loss with Mack's model

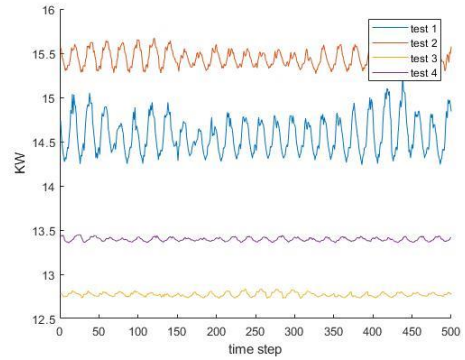


Fig 5. Windage loss with Mack's modified model

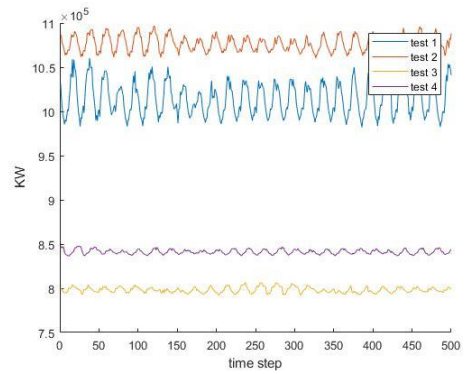


Fig 6. Windage loss with Vrancik's model

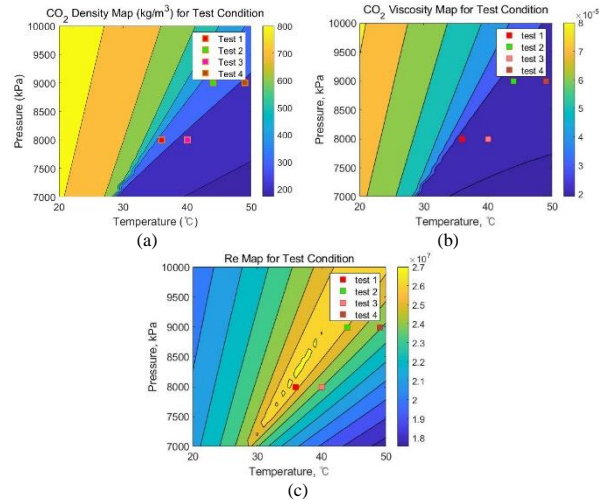


Fig 7. Description of the test condition; (a) Density, (b) Viscosity ( $\text{kg m}^{-1} \text{s}^{-1}$ ), (c) Reynolds number

### 3. Design of Windage Loss Experiments

#### 3.1 ABC loop

The ABC loop has key components of the S-CO<sub>2</sub> Brayton cycle: turbine, compressor, recuperator, pre-cooler, and heater as shown in Fig. 8. This system is designed to withstand more than 100 bar and 100  $^{\circ}$ C to test above the critical point of CO<sub>2</sub>.

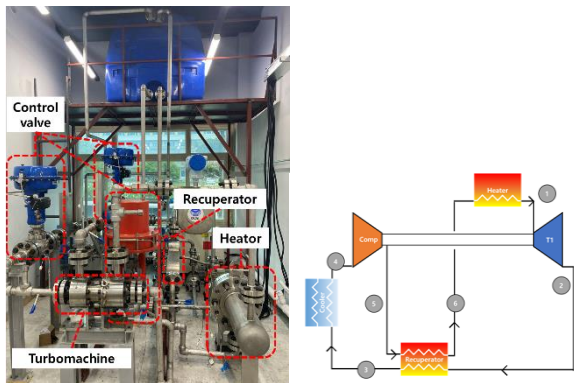


Fig 8. ABC loop and layout

### 3.2 External Loss Study with AMB Test Rig

The external losses can be calculated as below [5].

$$W_{loss,ext} = W_{input} - H_{CO_2} - Q_{water} - Q_{leak}$$

$W_{input}$  can be obtained from power analyzer and other terms are from the sensor data.  $W_{loss,ext}$  consists of the following losses.

$$W_{loss,ext} = W_{disk} + W_{windage} + W_{bearing}$$

Therefore, modeling the windage and other losses is required to separately investigate the term. For this, the AMB test rig in Fig. 9 is planned to be used. It is noted that the impeller is removed to omit disk loss in the external loss.

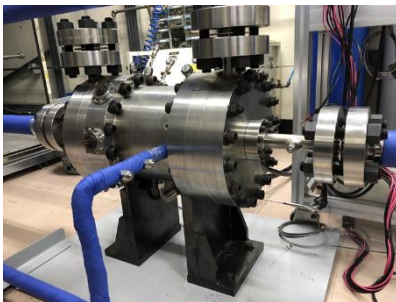


Fig 9. AMB test rig

## 3. Summary and Conclusions

In this paper, the windage loss models are reviewed and analyzed. As for the further works, the ABC loop in KAIST, which simulates the S-CO<sub>2</sub> power conversion system in an experimental scale, is planned to be used to investigate CO<sub>2</sub> properties effect on the windage loss. With this system, the windage loss test will be conducted for the windage loss model development.

## REFERENCES

- [1] Dostal, V., et al., A Supercritical Carbon Dioxide Cycle for Next Generation Nuclear Reactors, MIT-ANP-TR-100, 2004.
- [2] 안윤한, 배성준, and 이정익. "화력발전소 이용을 위한 초임계 이산화탄소 동력변환 계통 설계에 관한 연구." 유체기계 연구개발 발표회 논문집 (2013): 13-15.
- [3] Utamura, Motoaki, et al. "Demonstration of supercritical CO<sub>2</sub> closed regenerative Brayton cycle in a bench scale

experiment." Turbo Expo: Power for Land, Sea, and Air. Vol. 44694. American Society of Mechanical Engineers, 2012.

[4] Ahn, Yoonhan, et al. "Review of supercritical CO<sub>2</sub> power cycle technology and current status of research and development." Nuclear engineering and technology 47.6 (2015): 647-661.

[5] Kim, Seong Gu. "A design study of a supercritical CO<sub>2</sub> radial compressor by analyzing three-dimensional flow field, 3차원 유동 해석을 이용한 초임계 이산화탄소 압축기 설계 연구." (2018).

[6] Rosset, Kévin, and Jürg Schiffmann. "Extended Windage Loss Models for Gas Bearing Supported Spindles Operated in Dense Gases." Journal of Engineering for Gas Turbines and Power 142.6 (2020): 061010.

[7] Vrancik, James E. Prediction of windage power loss in alternators. Vol. 4849. National Aeronautics and Space Administration, 1968.

[8] Kim, Dokyu, SeungJoon Baik, and Jeong Ik Lee. "Instability Study of Magnetic Journal Bearing under S-CO<sub>2</sub> Condition." Applied Sciences 11.8 (2021): 3491.