



## Abstract

Numerical experiment of turbulent flow in a rod bundle using various anisotropic turbulence models has been performed. The anisotropic models used in this study are non-linear quadratic and cubic k-e models, and differential Reynolds stress model(RSM). The numerical experiment was conducted for fully developed turbulent flow in triangular and square rod bundles. The anisotropic models predicted the turbulence-driven secondary flow in the subchannel of rod bundle well but showed large difference in the magnitude depending on the model. They resulted in more accurate distributions of mean axial velocity and wall shear stress than standard k-e but their large differences were also noted. As for turbulence structure in the rod bundle, turbulence intensities in axial, radial and azimuthal directions were reasonably predicted in large flow region, but the very high azimuthal intensity in rod-gap region could not be predicted by any anisotropic model.

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. Carajilescov - Todreas<sup>1)</sup> 가 Vonka<sup>2)</sup> 2 (secondary flow) 3)-6) Rehme<sup>6)</sup> . , 2 가 (anisotropy) (large eddy) (flow pulsation) . Slagter<sup>7)</sup> 1-. Lee-Jang<sup>8)</sup> Lemos - Asato<sup>9)</sup> (eddy viscosity) 10) (CFD)

Speziale<sup>11)</sup>, Myong-Kasagi<sup>12)</sup>, Shih et al.<sup>13)</sup>Quadratic k-eCraft etal.<sup>14)</sup>Cubic k-eLaunder-Reece-Rodi(LRR)(RSM)<sup>15)</sup>Hooper-(RSM)<sup>15)</sup>Carajilescov-Todreas<sup>1)</sup>Hooper-

2.

Launder Spalding<sup>16)</sup> k - e 7 k e .

$$\boldsymbol{r}\frac{\partial k}{\partial t} + \boldsymbol{r}U_{j}\frac{\partial k}{\partial x_{j}} = \boldsymbol{t}_{ij}\frac{\partial U_{i}}{\partial x_{j}} - \boldsymbol{r}\boldsymbol{e} + \frac{\partial}{\partial x_{i}}\left(\left(\boldsymbol{m} + \boldsymbol{m} / \boldsymbol{s}_{k}\right)\frac{\partial k}{\partial x_{j}}\right),$$
(1)

가

$$\boldsymbol{r}\frac{\partial \boldsymbol{e}}{\partial t} + \boldsymbol{r}U_{j}\frac{\partial \boldsymbol{e}}{\partial x_{j}} = C_{\boldsymbol{e}1}\frac{\boldsymbol{e}}{k}\boldsymbol{t}_{ij}\frac{\partial U_{i}}{\partial x_{j}} - C_{\boldsymbol{e}2}\boldsymbol{r}\frac{\boldsymbol{e}^{2}}{k} + \frac{\partial}{\partial x_{i}}\left((\boldsymbol{m}+\boldsymbol{m}/\boldsymbol{s}_{\boldsymbol{e}})\frac{\partial \boldsymbol{e}}{\partial x_{j}}\right),$$
(2)

 $\boldsymbol{t}_{ij}$ 

$$\boldsymbol{t}_{ij} = -\boldsymbol{r}\overline{u_i'u_j'} = \boldsymbol{m}\left(\frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i}\right) - \frac{2}{3}\boldsymbol{r}\boldsymbol{k}\boldsymbol{d}_{ij}$$
(3)

$$\boldsymbol{m} = \boldsymbol{r} \boldsymbol{C}_{\boldsymbol{m}} \frac{k^2}{\boldsymbol{e}} \,. \tag{4}$$

 $k - \boldsymbol{e}$ 

$$C_m = 0.09, C_{e1} = 1.44, C_{e2} = 1.92, \boldsymbol{s}_k = 1.0, \boldsymbol{s}_e = 1.3$$
 (5)

(isotropy) 가 Quadratic Cubic

$$\mathbf{r}\overline{u_{i}'u_{j}'} = -\mathbf{m}S_{ij} + \frac{2}{3}\mathbf{r}k\mathbf{d}_{ij} + C_{1}\mathbf{m}\frac{k}{\mathbf{e}}\left(S_{ik}S_{kj} - \frac{1}{3}S_{kl}S_{kl}\mathbf{d}_{lj}\right) + C_{2}\mathbf{m}\frac{k}{\mathbf{e}}\left(\Omega_{ik}S_{kj} + \Omega_{jk}S_{kl}\right) + C_{3}\mathbf{m}\frac{k}{\mathbf{e}}\left(\Omega_{ik}\Omega_{jk} - \frac{1}{3}\Omega_{lk}\Omega_{lk}\mathbf{d}_{lj}\right)$$
(6)

.

.

$$\mathbf{r}\overline{u_{i}'u_{j}'} = -\mathbf{m}S_{ij} + \frac{2}{3}\mathbf{r}k\mathbf{d}_{ij} + C_{1}\mathbf{m}\frac{k}{e}\left(S_{ik}S_{kj} - \frac{1}{3}S_{kl}S_{kl}\mathbf{d}_{ij}\right) + C_{2}\mathbf{m}\frac{k}{e}\left(\Omega_{ik}S_{kj} + \Omega_{jk}S_{ki}\right) + C_{3}\mathbf{m}\frac{k}{e}\left(\Omega_{ik}\Omega_{jk} - \frac{1}{3}\Omega_{ik}\Omega_{ik}\mathbf{d}_{ij}\right) + C_{4}\mathbf{m}\frac{k^{2}}{e^{2}}\left(S_{ki}\Omega_{lj} + S_{kj}\Omega_{li}\right)S_{kl} + C_{5}\mathbf{m}\frac{k^{2}}{e^{2}}\left(\Omega_{il}\Omega_{lm} + S_{il}l\Omega_{lm}\Omega_{mj} - \frac{2}{3}S_{lm}\Omega_{mn}\Omega_{nl}\mathbf{d}_{ij}\right) + C_{6}\mathbf{m}\frac{k^{2}}{e^{2}}S_{ij}S_{kl}S_{kl} + C_{7}\mathbf{m}\frac{k^{2}}{e^{2}}S_{ij}\Omega_{kl}\Omega_{kl}$$
(7)

$$S_{ij} = \left(\frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i}\right), \quad \Omega_{ij} = \left(\frac{\partial U_i}{\partial x_j} - \frac{\partial U_j}{\partial x_i}\right) - \boldsymbol{e}_{ijk}\Omega_k$$
(8)

 $\mathbf{\Omega}_k$ 

. Table 1 가 Quadratic

Cubic

$$C_{m} = \frac{0.3}{1 + 0.35 (\max(S, \Omega))^{1.5}} \times \left( 1 - \exp\left[\frac{-0.36}{\exp(-0.75 \max(S, \Omega))}\right] \right),$$
(9)  
$$C_{1} = -0.1, C_{2} = 0.1, C_{3} = 0.26, C_{4} = -10C_{m}^{2}, C_{5} = 0, C_{6} = -5C_{m}^{2}, C_{7} = 5C_{m}^{2}$$

Table 1. Quadratic k - e

| Model                  | $C_{m}$                        | C <sub>1</sub>                  | C <sub>2</sub>               | C <sub>3</sub>               |
|------------------------|--------------------------------|---------------------------------|------------------------------|------------------------------|
| Speziale(1987)         | 0.09                           | -0.1512                         | 0.0                          | 0.0                          |
| Myong and Kasagi(1990) | 0.09                           | 0.275                           | 0.2375                       | 0.05                         |
| Shih et al.(1993)      | $\frac{2/3}{1.25+S+0.9\Omega}$ | $\frac{0.75/C_{m}}{1000+S^{3}}$ | $\frac{3.8/C_{m}}{1000+S^3}$ | $\frac{4.8/C_{m}}{1000+S^3}$ |

S Ω (strain rate) (vorticity) .

Launder - Reece - Rodi Navier - Stokes (RSM)

e

 $\boldsymbol{t}_{ij}$ 

$$\frac{\partial \boldsymbol{t}_{ij}}{\partial t} + \boldsymbol{U}_{k} \frac{\partial \boldsymbol{t}_{ij}}{\partial x_{k}} = -\boldsymbol{t}_{ik} \frac{\partial \boldsymbol{U}_{j}}{\partial x_{k}} - \boldsymbol{t}_{jk} \frac{\partial \boldsymbol{U}_{i}}{\partial x_{k}} + \frac{2}{3} \boldsymbol{red}_{ij} - \boldsymbol{\Pi}_{ij} + \boldsymbol{C}_{s} \frac{\partial}{\partial x_{k}} \left( \boldsymbol{t}_{im} \frac{\partial \boldsymbol{t}_{jk}}{\partial x_{m}} + \boldsymbol{t}_{jm} \frac{\partial \boldsymbol{t}_{ik}}{\partial x_{m}} + \boldsymbol{t}_{km} \frac{\partial \boldsymbol{t}_{ij}}{\partial x_{m}} \right) \right)$$
(10)

$$\boldsymbol{r}\frac{\partial \boldsymbol{e}}{\partial t} + \boldsymbol{r}U_{j}\frac{\partial \boldsymbol{e}}{\partial x_{j}} = C_{\boldsymbol{e}1}\frac{\boldsymbol{e}}{k}\boldsymbol{t}_{ij}\frac{\partial U_{i}}{\partial x_{j}} - C_{\boldsymbol{e}2}\boldsymbol{r}\frac{\boldsymbol{e}^{2}}{k} - C_{\boldsymbol{e}}\frac{\partial}{\partial x_{k}}\left(\frac{k}{\boldsymbol{e}}\boldsymbol{t}_{km}\frac{\partial \boldsymbol{e}}{\partial x_{m}}\right)$$
(11)

.

 $\Pi_{ij}$  - LRR <sup>15)</sup> Rotta <sup>17)</sup> (wall reflection) .

. RSM(LRR)

$$\Pi_{ij}^{(w)} = \left\{ 0.125 \frac{\boldsymbol{e}}{k} \left( \boldsymbol{t}_{ij} + \frac{2}{3} \boldsymbol{r} k \boldsymbol{d}_{ij} \right) - 0.015 \left( P_{ij} - D_{ij} \right) \right\} \frac{k^{3/2}}{\boldsymbol{e} n}$$
(12)

$$P_{ij} = \boldsymbol{t}_{im} \frac{\partial U_j}{\partial x_m} + \boldsymbol{t}_{jm} \frac{\partial U_i}{\partial x_m}, \quad D_{ij} = \boldsymbol{t}_{im} \frac{\partial U_m}{\partial x_j} + \boldsymbol{t}_{jm} \frac{\partial U_m}{\partial x_i}$$
(13)

 $C_1 = 1.8, C_2 = 0.60, C_s = 0.11, C_e = 0.18$ (14)

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•

3.

3.1



Figure 1.

(25 x 45)



Figure 2.



3.2

| 4 <sup>18)</sup> | - ,       | k – <b>e</b> | CFX-4   | C   | FD         | CFX-             |
|------------------|-----------|--------------|---------|-----|------------|------------------|
| CFX-4            | SIMPLE    |              | SIMPLEC | 가   |            |                  |
|                  | (wall fun | ction)       |         | . ( | under - re | elaxation)       |
| (residual)       | 0.001%    |              |         |     |            | 10 <sup>-4</sup> |
| 가                |           | (Uo          | )       |     |            |                  |
| 27000(           | ) 207600  | (            | ) .     |     |            |                  |

4.

4.1

Figure 3 2 가 2 Gap 2 0.8% (Speziale), 0.6% (Myong-Kasagi), 0.1%(Shih et al.), 0.15%(Cubic) 1.3%(RSM) . Carajilescov - Todreas 2 가 0.67% Speziale Myong-. 가 2 Shih et al. Cubic Kasagi RSM(LRR) 19) Figure 4 MOSA3D . Shih Quadratic k - eCraft Cubic k - ek - eGap 가 . Speziale Myong-Kasagi Quadratic k - eGap CFD MOSA3D , RSM(LRR) k - eGap Figure 5 Gap 가 *k*−*e* Cubic k - e. . Shih Quadratic k - eCubic k - e. Speziale Quadratic k - eSpeziale Myong-Kasagi RSM(LRR) Gap . Figure 6  $Gap(\theta=0)$ 가 (θ=30) . Shih Quadratic k - eCubic k - e*k*−*e* Speziale Myong-Kasagi Quadratic k - eθ=25 가 . RSM(LRR) θ=25 (θ=30) .

4.2

Figure 7 Quadratic/Cubic k-e RSM(LRR) 2 . 2 Gap 2 1.1%(Speziale), 0.9%(Myong-Kasagi), 0.18%(Cubic) 2.2%(RSM) Quadratic Cubic 2 . Shih 2 Carajilescov-Todreas<sup>1)</sup>가 Vonka<sup>2)</sup> (P/D=1.123) 가 0.67% 가 0.2% (P/D=1.3) 2 . 2 P/D=1.107 . Speziale Myong-Kasagi Quadratic 2 .  $Gap(\theta=0)$  ( $\theta=45$ ) (mean flow) Fig. 8 . Cubic Gap . Shih Quadratic Cubic . Myong-Kasagi Quadratic (Speziale 가 ) Gap 10% • , RSM(LRR) k - eGap . Figure 9 가  $Gap(\theta=0)$ . Cubic k-ek - e(Shih Quadratic ). Speziale Myong-Kasagi Quadratic k-eGap 15% θ=37 5% . RSM(LRR) Gap θ=30 (θ=45) Figure 10 Gap Gap u', v', w' . ,  $u_t$ . . Speziale ( w' ) . Myong-Kasagi ( u' ) Gap 가 ( v' ) . Cubic

|       | . RSM(I     | _RR)      | -                   |                | -            |              |            |     |
|-------|-------------|-----------|---------------------|----------------|--------------|--------------|------------|-----|
|       |             | k         | <b>k</b> – <b>e</b> |                |              |              |            |     |
|       | Figure 11   |           |                     |                | Gap          |              |            |     |
|       | . Figure 10 |           | Gap                 |                |              |              |            |     |
|       | . Spezia    | le        |                     |                | ( u' )       |              |            |     |
|       |             |           |                     |                |              | . Gap        |            |     |
|       |             | ( w' )    | 가                   |                | . My         | /ong-Kasagi  |            |     |
|       | . Cubic     |           |                     |                |              |              |            |     |
| RSM(  | (LRR)       | 가         | 가                   | 가              |              |              |            |     |
|       | Figure 12   | 2         |                     |                |              |              |            |     |
|       |             | Gap       |                     |                |              |              |            | Gap |
|       |             |           |                     |                | . Shih       | Quadratic    | Cubic      |     |
|       |             |           |                     |                | Speziale     | Myong-Kasa   | gi         |     |
|       |             |           |                     | . F            | RSM(LRR)     |              |            |     |
|       |             |           |                     |                |              |              |            |     |
| _     |             | 가         | у/у ^               | >0.6           |              | 가            |            |     |
| Gap   |             | 가         | Speziale            | Myor           | ng-Kasagi    | Shih         | Quadratic  |     |
| Cubic |             |           | -1                  |                |              |              |            | •   |
| RSM(  | (LRR)       | 가         | 가                   |                |              |              |            |     |
| F     |             |           |                     |                |              |              |            |     |
| э.    |             |           |                     |                |              |              |            |     |
|       |             |           |                     |                |              |              |            |     |
|       |             |           |                     |                |              |              |            |     |
|       |             |           |                     |                |              |              |            |     |
| 1)    |             |           |                     | 2              |              | k – <b>e</b> |            |     |
| 2)    | Speziale M  | vong-Kasa | di Quad             | ratic <i>I</i> | х — р        | Shih Qua     | dratic k-e |     |
| _,    | Cubic $k-e$ | yong naoa | 9. 4444             |                | 2            |              |            |     |
|       |             |           |                     |                |              |              |            |     |
| 3)    | Myong-Kasa  | gi        |                     |                |              |              |            |     |
|       | Speziale    |           |                     |                |              | 2            |            |     |
|       |             |           |                     |                |              |              |            |     |
| 4)    |             |           | (RSM)               |                | k – <b>e</b> |              |            |     |

| 5)  | Gap             |                     |
|---|-----------------|---------------------|
|   |                 |                     |
|   |                 |                     |
|   |                 |                     |
|   |                 |                     |
|   |                 |                     |
|   |                 |                     |
|   |                 |                     |
|   |                 |                     |
| U   |                 |                     |
| $U_{o}$   | / 5             |                     |
| u <sub>t</sub>                                      | (1)             | rictional velocity) |
| y<br>$y^{2}$ , $\hat{y}$                            |                 |                     |
| 5,5   |                 |                     |
| $\boldsymbol{d}_{ij}$                               | kronecker delta |                     |
| щ   |                 |                     |
| r   |                 |                     |
| $\boldsymbol{S}_k, \boldsymbol{S}_{\boldsymbol{e}}$ | Prandtl         |                     |
| q   |                 |                     |
|   |                 |                     |

<sup>6.</sup> 

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Figure 8.



Figure 9.



Figure 10.

 $Gap(\theta=0)$ 



Figure 12.

Gap(θ=0)

(θ=45)