

Coarse Mesh Finite Difference Method with Interface Coupling Coefficient Correction for Real Time Analysis of Space-Time Dependent Neutron Diffusion Equation

305-353

150

2 3

4

100 pcm ,

1 % ,

Abstract

A 4-cycle real time analysis methodology was developed to solve 2-group 3-dimensional space-time dependent neutron diffusion equation, using coarse mesh finite difference method with interface coupling coefficient correction. Comparisons with higher order nodal method were performed by steady state and transient analyses of Yonggwang unit 1 cycle 15 reactor. For the steady state core within the typical operating moderator temperature range, the differences of core reactivity and radial power distribution are less than 100 pcm and 1 %, respectively, and no attentive difference was observed in the results of the transient analyses coupled with system calculations.

I.

가

NPA (Nuclear Plant Analyzer)

(FDM - Finite Difference Method)

4

FDM

3

가

가

MASTER

MASRS

[1]

MASTER

RETRAN

[2]

가

가

RETRAN

MASTER

0.25

4

가

ANC^[3]

ROCS^[4]

가

(CMFD - Coarse Mesh Finite Difference)^[5]

4

0.25

CMFD

가

FDM

가

FDM

(NLANM-Non-Linear Analytic Nodal Method)^[6]

(ANM)

(CNCC - Corrective Nodal Coupling Coefficient)

(ICCC - Interface Coupling Coefficient

Correction)

ICCC NLANM

CMFD

NLANM

ICC

NLANM

1 15 [7]

ANC

II.

2 3

$$\frac{1}{v_g} \frac{d\phi_g}{dt} = \begin{cases} (1-\beta)\psi + S_d - L_1 - \Sigma_{r1}\phi_1, & g=1 \\ \Sigma_{12}\phi_1 - L_2 - \Sigma_{r2}\phi_2, & g=2 \end{cases} \quad (1)$$

, ψ , S_d

g

가

3

$$L = \sum_{u=x,y,z} L_u = \sum_{u=x,y,z} \frac{1}{h_u} (J_u^r - J_u^\ell) \quad (2)$$

 h_u , J_u^ℓ J_u^r

(current)

(FDM)

(2)

가

u

(interface current) \tilde{J}_u

$$\tilde{J}_u = -\tilde{D}_u (\phi^r - \phi^\ell) \quad (3)$$

, ϕ^ℓ ϕ^r

u

 \tilde{D}_u
 D_u^ℓ D_u^r , h_u^ℓ h_u^r

$$\tilde{D}_u = \frac{2D_u^r D_u^\ell}{D_u^r h_u^\ell + D_u^\ell h_u^r} \quad (4)$$

, (CMFD) (3)

$$\tilde{J}_u = -\tilde{D}_u(\phi^r - \phi^\ell) - \hat{D}_u(\phi^r + \phi^\ell). \quad (5)$$

$$\hat{D}_u \quad \tilde{J}_u^H$$

$$\hat{D}_u = \frac{\tilde{J}_u^H + \tilde{D}_u(\phi^r - \phi^\ell)}{\phi^r + \phi^\ell}. \quad (6)$$

m u (2) (5)

$$L_u^m = a_u^\ell \phi^{m-} + a_u^m \phi^m + a_u^r \phi^{m+}. \quad (7)$$

$m-$ $m+$ m , ℓ r m
 a

$$\begin{aligned} a_u^\ell &= -\frac{1}{h_u^m} (\tilde{D}_u^\ell - \hat{D}_u^\ell), \\ a_u &= \frac{1}{h_u} [\tilde{D}_u^\ell + \tilde{D}_u^r + \hat{D}_u^\ell - \hat{D}_u^r], \\ a_u^r &= -\frac{1}{h_u^m} (\tilde{D}_u^r + \hat{D}_u^r). \end{aligned} \quad (8)$$

CMFD (5) (7)
 (1) (tri-diagonal) FDM
 가 (outer iteration) 가 (6)
 (ICCC) FDM
 ICCC
 가 가 (6) (4)

$$\hat{D} = \frac{\tilde{D}h_u}{\phi^r + \phi^\ell} \left(\left. \frac{d\phi}{du} \right|_S^H - \frac{\phi^r - \phi^\ell}{h_u} \right). \quad (9)$$

가

$$\left. \frac{d\phi}{du} \right|_S^L = \frac{\phi^r - \phi^\ell}{h_u} \quad (10)$$

가

$$\frac{\hat{D}}{\tilde{D}} = \frac{h_u}{\phi^r + \phi^\ell} \left(\left. \frac{d\phi}{du} \right|_S^H - \left. \frac{d\phi}{du} \right|_S^L \right) \quad (11)$$

ICCC

$$\hat{D} / \tilde{D}$$

$$\begin{aligned} \Sigma = \Sigma(B_0, T_{f0}, D_{m0}) &+ \frac{\partial \Sigma}{\partial B} \Delta B + \frac{\partial \Sigma}{\partial \sqrt{T_f}} \Delta \sqrt{T_f} + \frac{\partial \Sigma}{\partial D_m} \Delta D_m \\ &+ \Delta \Sigma_{CR}(B_0, T_{f0}, D_{m0}) + \frac{\partial \Delta \Sigma_{CR}}{\partial B} \Delta B + \frac{\partial \Delta \Sigma_{CR}}{\partial \sqrt{T_f}} \Delta \sqrt{T_f} + \frac{\partial \Delta \Sigma_{CR}}{\partial D_m} \Delta D_m \end{aligned} \quad (12)$$

B, T_f, D_m , , $\Delta \Sigma_{CR}$, 0 , 가

ICCC

. ICC

(12)

가

2

ICCC

1

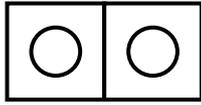
4가

ICCC

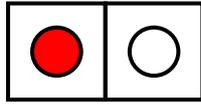
$$\frac{\hat{D}}{\tilde{D}} = (1-C) \left(\frac{\hat{D}}{\tilde{D}} \right)_0 + C \left(\frac{\hat{D}}{\tilde{D}} \right)_L \quad (13)$$

C

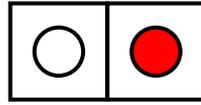
L



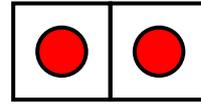
L=0



L=1



L=2



L=3



1.

ICCC 3

(CMFD_H)

NLANM

ICCC

ICCC

(CMFD_C)

III.

가

CMFD_C

CMFD_H

1 15

150 MWD/MTU

2

가.

ANC

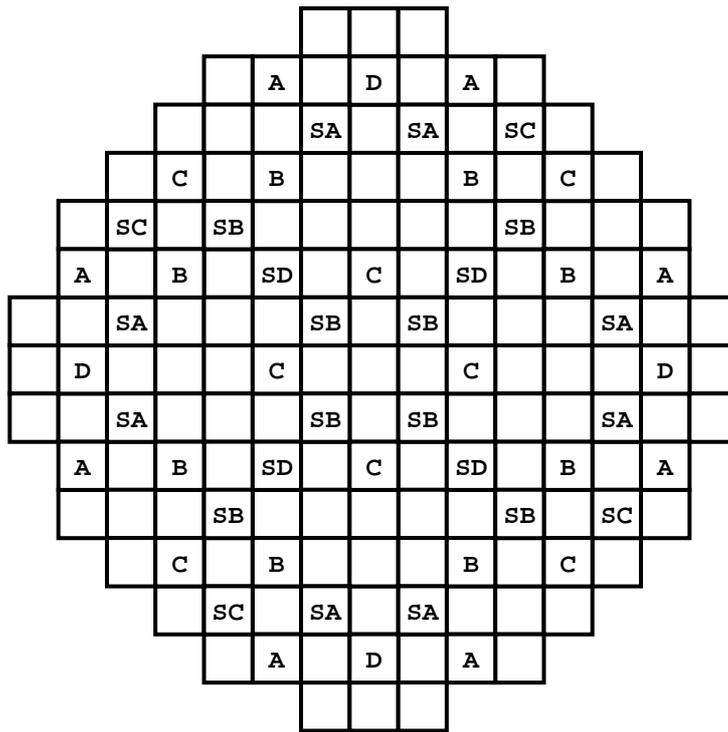
(12)

ANC

1

1

가



2. 1

1. ANC

		(%)	(ppm)	(g/cm ³)	(°C)
1		0	500	0.74335	291.7
2	1	0	1000	0.74335	291.7
3	2	0	1	0.74335	291.7
4	1	100	500	0.74335	291.7
5	2	200	500	0.74335	291.7
6	1	0	500	0.59572	320.0
7	2	0	500	0.64768	320.0
8	3	0	500	0.68008	320.0
9	4	0	500	0.81195	250.0
10	5	0	500	0.89646	180.0
11	6	0	500	0.96536	100.0
12	7	0	500	0.99999	27.0

(12)

ICCC
 CMFD_H
 가
 CMFD_C
 CMFD_H
 ICCG가
 가
 CMFD_C
 ICCG
 가
 1.0
 가
 CMFD_C
 CMFD_H
 ICCG가
 CMFD_C
 CMFD_H
 가
 가
 가
 가

2. CMFD_C CMFD_H

	(PCM)		(P>1.0) (%)	
	ARO	ARI	ARO	ARI
	7.1	32.7	0.57	0.86
1	3.4	23.7	0.31	0.84
2	16.7	50.1	0.90	1.08
1	16.3	37.0	0.74	1.07
2	16.2	35.7	0.72	1.06
1	-43.4	-99.0	1.88	1.48
2	-25.9	-50.5	1.15	1.31
3	-15.1	-22.5	0.31	1.19
4	36.6	96.4	1.96	1.47
5	88.5	189.1	3.93	3.56
6	155.5	287.6	5.85	3.68
7	202.8	350.7	5.07	4.45

가 250 °C

가 100 pcm , 가 1 %

500 pcm

5%

ARO

. CMFD_C CMFD_H

1.7 pcm

3 4

. , 50%

Bank D 가 50%

3.4 pcm

5 6

1.0

0.5 %

가

가

가

CMFD_C

가 가

CMFD_H

가

가

RETRAN

Dynamic-link Library (DLL)

. RETRAN

6 1

3

3

RETRAN 1

/

Bank SD

가

CMFD_H

CMFD_C

694.7 pcm

692.0 pcm

1.14 \$

0.1

가

0.002

7

CMFD_H

CMFD_C

78.82 % 77.14 %

0.440

0.448

가

1 %

D, C

가

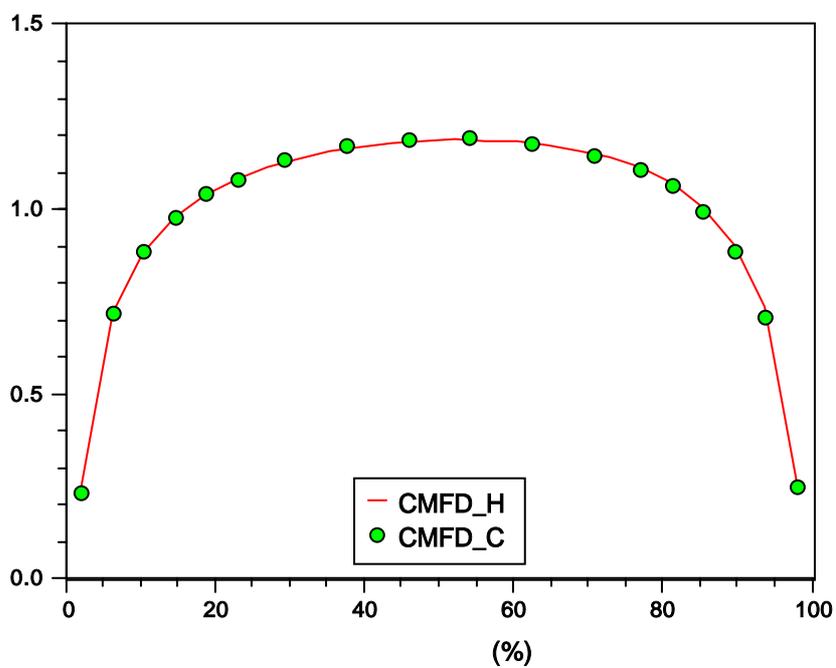
B가 50 %

50 %

0.904	1.215	1.049	1.258	1.035	1.206	0.782	0.451
0.903	1.213	1.047	1.260	1.035	1.210	0.783	0.454
0.1	0.2	0.1	-0.1	0.0	-0.3	-0.1	-0.7
	0.961	1.234	1.279	1.291	1.265	1.222	0.345
	0.959	1.229	1.277	1.293	1.264	1.216	0.345
	0.1	0.4	0.2	-0.2	0.1	0.4	0.0
		1.273	1.328	1.248	1.167	1.010	
		1.270	1.330	1.247	1.173	1.007	
		0.2	-0.2	0.1	-0.5	0.3	
			1.080	0.808	0.332		
			1.084	0.810	0.333		
			-0.4	-0.2	-0.2		
				0.315			
				0.314			
				0.1			

CMFD_C
CMFD_H
%

3. ARO

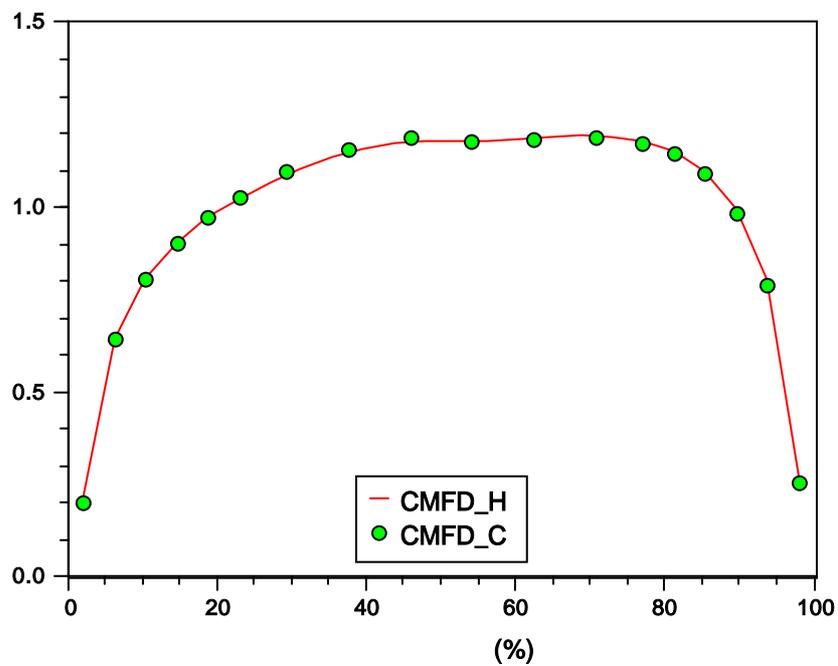


4. ARO

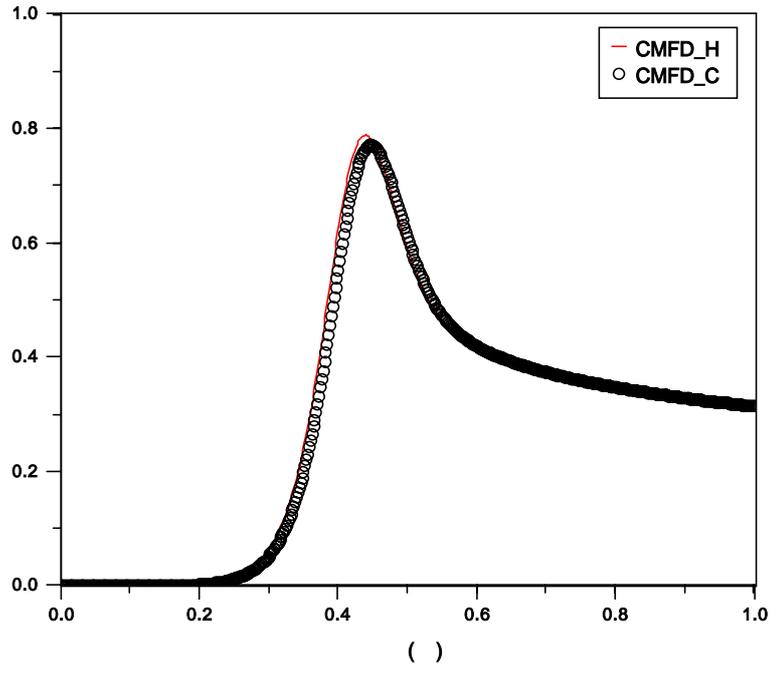
0.926	1.256	1.082	1.299	1.035	1.143	0.576	0.366
0.924	1.257	1.079	1.302	1.035	1.148	0.577	0.366
0.2	-0.1	0.3	-0.2	0.2	-0.5	-0.2	-0.0
	0.988	1.284	1.330	1.315	1.239	1.132	0.298
	0.985	1.280	1.327	1.319	1.239	1.127	0.297
	0.3	0.3	0.2	-0.3	0.0	0.4	0.1
		1.334	1.389	1.285	1.170	0.980	
		1.331	1.393	1.284	1.177	0.978	
		0.2	-0.3	0.1	-0.5	0.3	
			1.110	0.808	0.320		
			1.114	0.809	0.319		
			-0.4	-0.1	0.2		
				0.309			
				0.308			
				0.4			

CMFD_C
CMFD_H
%

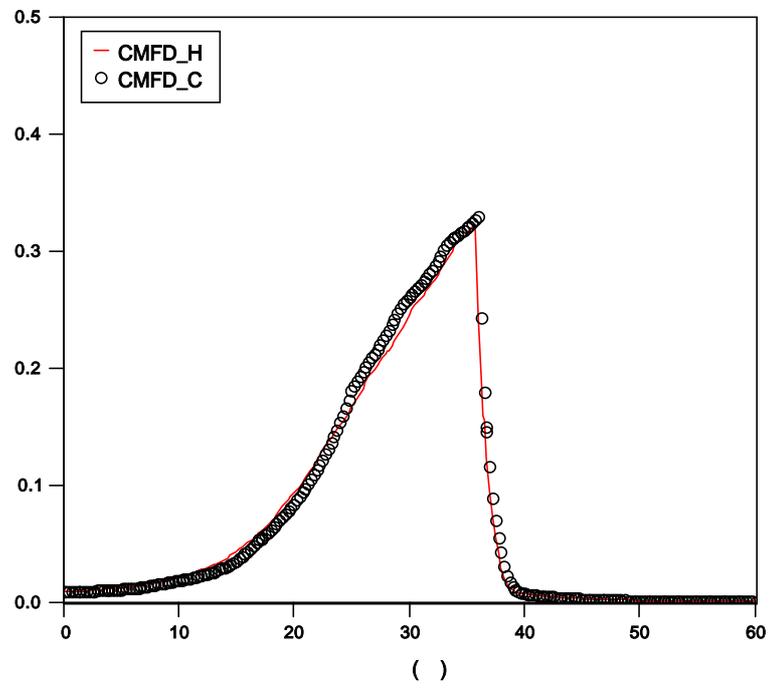
5. 50 % Bank D 50 %



6. 50 % Bank D 50 %



7.



8.

1.8 cm . 0.25

8 . /

CMFD_H CMFD_C 33.75 34.00 가

가 35.75 36.00 .

32.41% 33.01 %

CMFD_C ICC

가

4 .

가

가 가

가

9 CMFD_H CMFD_C 0.25

CMFD_H

0.05 . 0.25

0.05 , CMFD_C

10 가 3 CMFD_H CMFD_C

CMFD_C

4.7 ,

3

0.25 가 .

IV.

(ICCC)

가

4

3 ICC 1 15

가 100 pcm, 1%

350 pcm

500 pcm ,

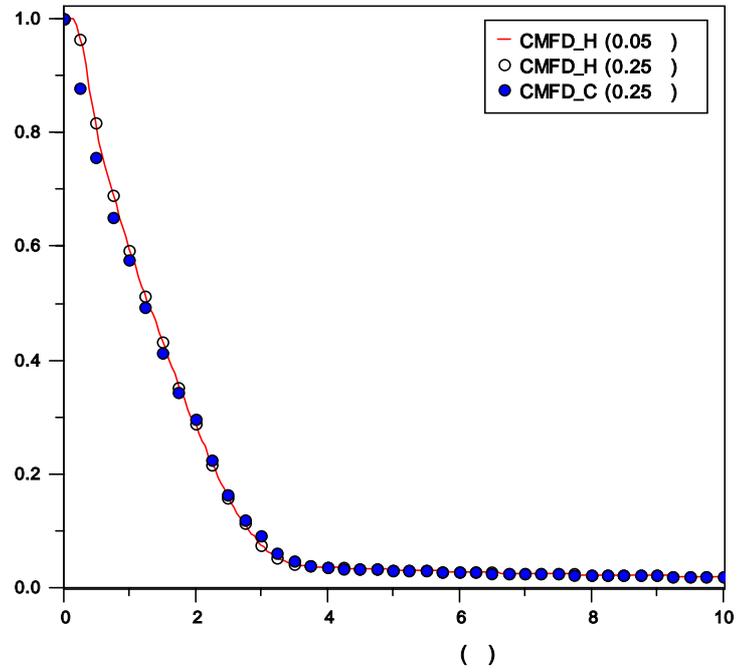
5% . /

가 .

NPA

가

1 15



9.

3.

CMFD_H	0.016	0.062	0.438	0.516
CMFD_C	0.016	0.062	0.094	0.172

() Intel Pentium IV 3 GHz CPU , () :

1. J.J. Jeong et al., "MARS/MASTER Solution to OECD Main Steam Line Break Benchmark Exercise III," *J. Korean Nucl. Soc.*, 32, 214 (2000).
2. , "RETRAN-MASTER-TORC ,," KAERI/TR-2292/2002.
3. T.Q. Nguyen et al., "Qualification of the PHOENIX-P/ANC Nuclear Design System for Pressurized Water Reactor Cores," WCAP-11596-P-A (1988).
4. "User's Manual for ROCS," CE-CES-4 Rev. 11-P (1996).
5. T. M. Sutton and B. N. Aviles, "Diffusion Theory Methods for Spatial Kinetics Calculations," *Progress in Nuclear Energy*, Vol. 30, No. 2, pp. 119-182 (1996).
6. H.G. Joo et al., "PARCS, A Multi-Dimensional Two-Group Reactor Kinetics Code Based on the Nonlinear Analytic Nodal Method," PU/NE-98-26 (1998).
7. D.I. Chang et al., "The Nuclear Design and Core Physics Characteristics of the Yonggwang Nuclear Power Plant Unit 1 Cycle 15," KNF-Y1C15-03010 (2003).