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*A Study on the Condition of Single Crystal Neutron Experiment

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Abstract

The reciprocal space method of increasing the signal to background ratio in X-ray diffraction work with single crystal is extended to the case of equatorial neutron diffraction works. The formulae of optimum width of the detectors with the various experimental methods are derived.

요 약

X-선회절 실험에서 불필요한 관측치에 대한 실제실험치의 비율을 높이기 위한 역격자공간방법을 중성자의 경우에 응용하고 여러가지 실험방법을 택하는 경우에 적합한 검출기의 크기에 대한 관계식을 도출하였다.

1. Introduction

Among the factors which have to be considered in setting the conditions of experiments with counter diffractometers, there are two main things as follows: (i) how to increase the signal to background ratio in the measurement of integral intensities, (ii) how to save the time obtaining the same degree of accuracy.

The effort for finding the optimum condition of the experimental methods with the above considerations has been continued for x-ray and neutron cases separately. In x-ray case, the so called reciprocal space method has been used usually:¹⁻³⁾

Kheiker³⁾ recently studied on the errors in the measurements of integrated intensities with

various methods using non-monochromatic radiation. He has shown that the errors are determined by: (i) the magnitude of the scan volume in reciprocal space, (ii) incorrect determination of the background, *etc.* On the other hand, the method of tracing the paths of neutrons in a certain experimental geometry have been used in neutron case⁴⁻⁶⁾. This technique may be called "tracing method." In these works, have been derived the influence of the collimator parameters (typically the angular divergence) on the luminosity and the resolution in neutron single crystal diffractometry on the basis of Saylor's hypothesis⁴⁾. Caglioti *et al*^{5, 6)} have developed general expressions for the resolution and luminosity of the diffraction peaks for single crystal samples.

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2. Diffraction Profile

To determine the structure factors in diffraction works with single crystals, reflected integral intensities are measured usually. The formula for this intensity may be written as follows:

$$I_{int} = \int_{d\omega} J_o(\omega) d\omega \quad (1)$$

where $J_o(\omega) = J_a(\omega) J_p(\omega) J_s(\omega) J_\lambda(\omega) J_m(\omega)$,

ω : the angle in the real space

$J_a(\omega)$: the diffraction profile,

$J_s(\omega)$: the dispersion profile of the incident rays,

$J_\lambda(\omega)$: the spectrum of the incident ray,

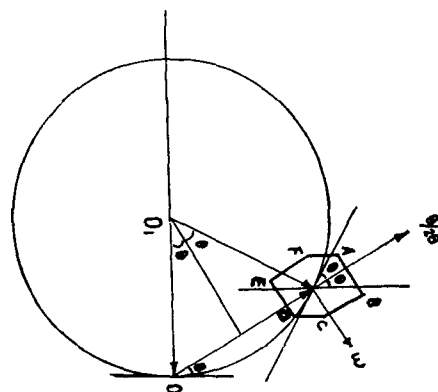
$J_m(\omega)$: the mosaicity of the sample,

$J_p(\omega)$: the profile caused by the shape and dimension of the sample,

and $J_o(\omega)$ is the final profile caused by the rotation of goniometer. When the independency among the factors in the integrand is considered, equation (1) is reduced to

$$I_{int} = \text{const} \int J_a(\omega) d\omega. \quad (2)$$

It is possible to compare the final diffraction profiles with the experimental results in order to determine the properly moving intervals of the detector and the sample in the measurement. It is also possible to compare the results of various methods and to carry out the error calculations.



$$AB + H\lambda M + 2H\lambda P_{11}\sin\theta, \quad BC = H\lambda\lambda + 2P_{11}\cos^2\theta, \\ CD = X$$

Fig. 1. Graphical representation of integrated intensity measurement in the equatorial case

3. Construction of Comparing Methods in Reciprocal Space

There is several methods for comparing the results of integral intensity measurements using various methods. The comparing method which has been derived by working in reciprocal space is very neat. The equatorial section of an Ewald sphere involved in the measurement of integral intensity is shown in Fig. 1.

The meanings of various notations in Fig. 1 are as follows:

$H\lambda$: a lattice vector in reciprocal space ($H\lambda = 2\sin\theta$),

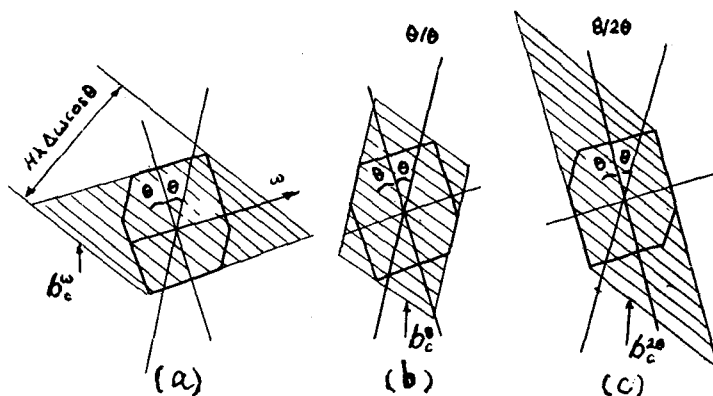


Fig. 2. Scanning volumes for different scanning methods

as mentioned above. The results such as equations (3) to (7) are adequate for this case with the substitution $x+x_0$ instead of x_0 .

If $x > x_0$, the scanned volume is slightly different from Fig. 1 and is shown as in Fig. 3.

Let's ignore the mosaic spread of the monochromator and the size of the sample for convenience. All the results for b_c^ω , $b_c^{\theta/2\theta}$, $b_c^{\theta/2\theta}$, and for h_c turn out to be as the same as equations (3) to (7) respectively. Specially, when the scanning method along the direction of B D is chosen, the b_c can be made small by applying the relation between the rotational speed of the sample ω and that of the detector γ as follows:

$$\frac{\omega}{\gamma} = \frac{1}{1 + 2 \cot \theta_0 \tan \theta_0} \quad (8)$$

The width of the detector and the measuring interval should be as the following:

$$b'_c = 2M + x_0 + 2p \quad (9)$$

$$\Delta\omega = x(1 + \cot \theta_0 \tan \theta) + M + x_0 + p. \quad (10)$$

5. Results and Discussion

The method of taking diffraction data can be chosen by taking the smallest detector width

calculated by equations (3) to (5). In author's opinion, the problem of choosing optimum condition for diffraction experiment may be solved more elaborately if the above discribed reciprocal method and the tracing method may be combined. The expression for the full width at half maximum of the diffraction peaks for single crystal sample, $A_{\frac{1}{2}}$, has been given by Caglioti *et al*^{5, 6)}. They have also derived the formula for the luminosity of the diffraction peaks, L ^{5, 6)}. The formulae for detector width, equations (3) to (5), and the above $A_{\frac{1}{2}}$ and L may be combined.

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