Coupling of Mesh Generator Code (VEGA) to Two-dimensional Tokamak Plasma Transport Code (C2)

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Abstract – By upgrading the mesh generator, VEGA, to VEGA2.0 and developing a bridge code, a 2-D core-edge coupled modelling package consist of VEGA2.0 and the two-dimensional tokamak plasma transport code C2 is complete for analysis of the entire region of the poloidal plane of the tokamak plasma. The upgrade is conducted with the reconstruction of the entire code in C++ programming language and modification for the flexibility. In this procedure, VEGA2.0 has an organized data structure and system layout, and a robustness in various configurations of plasma. In the following procedure, a bridge code is made with the matching each grid storage format of the two codes and adding the additional data that C2 needs. The VEGA2.0 is verified with the former VEGA in KSTAR Connected Double Null (CDN) plasma by the grid quality factors. In Last, plasma simulation results in KSTAR CDN plasma conducted by this completed core-edge coupled modelling package are presented.

I. INTRODUCTION

Computational simulation of the tokamak plasma transport can be broadly divided into two different areas, core and edge/Scrape-Off Layer (SOL) region. The transport in the core region is dominated by the parallel transport along the magnetic field lines due to high temperatures and it can be described on the magnetic flux surface with surface averaged one-dimension (1-D) quantities [1]. On the other hand, the two-dimensional (2-D) effect should be considered in the edge/SOL region because the parallel and the perpendicular transport are comparable and the wall structures such as the divertor and the first wall should be considered [2].

Conventionally, two approaches have been used to simulate the plasma transport in the coupled core and edge/SOL regions where these distinct features coexist. The first approach is integrating the codes designed to solve each core or edge/SOL region in a corresponding manner to simulate the entire plasma region. Packages such as OMFIT [3], ITM [4], and JINTRAC [5] belong to this way, and most of them get the plasma status 1-D in the core and 2-D in the edge/SOL region. In this case, it is important to maintain numerical self-consistency at the boundary between the two regions.

The second one is to simulate in the entire poloidal plane two-dimensionally through a set of inherent equations. C2 [6] is one of the codes using this approach where the multi-fluid MHD equations with the modified neoclassical heat and momentum diffusivities are solved. In this case, coupling at the boundary between the two regions (core and edge/SOL) is inherently made because this code treats the plasma in the same manner regardless the region. Therefore, it is convenient to study the various effects of the plasma interaction at the divertor or Plasma Facing Component (PFC) on the core plasma with this C2.

However, the computational domain, grid, is static in a whole process of time-varying plasma simulations in C2. Because the boundary area of the subjected core-edge/SOL phenomena changes over time, the grid needs to adapt this variation.

According to this demand, a VEctor-following Grid generator for Adaptive mesh (VEGA) has been developed [7]. The characteristic of this code is that it automatically defines the magnetic configuration of the given plasma equilibrium data and generates the grid using the vector-following method. A time-dependent coupled core-edge/SOL simulation is feasible by integrating VEGA and C2 as a core-edge coupled modelling package. However, VEGA had several limitations to be described in the next chapter which needs to be resolved for broader applications and rigid simulations.

In addition, as C2 and VEGA grid formats are different and C2 uses additional data, a bridge code is required to link them in order to complete the core-edge coupled modelling package. Therefore, the grid generator VEGA is upgraded to VEGA2.0 in this work.

The paper is organized as follows. Firstly, the limitations of former VEGA are addressed. Then, upgrade of VEGA, VEGA2.0 is described in detail. Next, the bridge code is introduced. In chapter III, the results of grid generated by VEGA2.0 are presented and compared with the result of former VEGA. The results of a plasma simulation by using the core-edge coupled modelling package are followed. Finally, the summary and conclusion are presented in chapter IV.

II. DESCRIPTION OF THE ACTUAL WORK

In this chapter, two processes are introduced to establish the core-edge coupled modelling package. First, VEGA is upgraded to VEGA2.0 by solving the internal limitations.
Second, a bridge code to link this VEGA2.0 with C2 is developed. The details are described below.

1. Upgrade of VEGA to VEGA2.0

The former VEGA has several limitations. Firstly, it is coded in MATLAB [8]. MATLAB is a very flexible language versatile and easily analyzable, but has weak points of incompatibility with other codes in a Linux system in a computational cluster and slow computation speed because all modules are loaded every time the program is executed. In addition, the input and the output parts of the system process are missing, making it difficult to connect with other codes. Also, it is not easy to interpret the code and manage the variables because the data is not organized.

Secondly, the former VEGA can deal with only specific magnetic configurations. It can generate a grid for Connected Double Null (CDN) and Single Null (SN) only, thus its application can be limited when dealing with other configurations. For example, the constraint applied when the grid is twisted near X-point or divertor plates are too localized, or the number and the accuracy of the first points in the separatrix lines from the X-point are limited.

Therefore, the following procedures and methods are employed to overcome these limitations.

A. Re-construction to C++ Programming Language

There is a need to reconstruct the former VEGA in other programming languages in order to overcome the compatibility problems. The programming languages used in other conventional codes are listed in Table 1. As shown FORTRAN has been used extensively that has been developing for long, such as ASTAR [1] or B2.5 [2].

However, relatively recently developed C2 is coded in the C++ programming language, so VEGA to be coupled with this code is also reconstructed in this C++ language. The advantage of C++ is that it is suitable for Linux systems and has a wide range of applications because it has already been dealt with in a lot of areas, and it is also good for connecting with other codes.

Since the reconstruction in C++ language, VEGA2.0 has been largely changed internally. One of them is an organized data structure. Due to the inherent property of each code language, the data structures of the former VEGA and VEGA2.0 are different. As shown in Fig. 1, the variables are not organized in the former VEGA, thus users must give and take every variable when they use functions in the code.

<table>
<thead>
<tr>
<th>Code</th>
<th>Features</th>
<th>Language</th>
</tr>
</thead>
<tbody>
<tr>
<td>ASTAR [1]</td>
<td>1D Core solver</td>
<td>FORTRAN77</td>
</tr>
<tr>
<td>B2.5 [2]</td>
<td>2D Edge/SOL solver</td>
<td>FORTRAN77</td>
</tr>
<tr>
<td>KTRAN [9]</td>
<td>2D diverter solver</td>
<td>C Language</td>
</tr>
<tr>
<td>C2 [6]</td>
<td>2D Core-Edge solver</td>
<td>C++ Language</td>
</tr>
</tbody>
</table>

Table 1. List of codes sorted by their program language.

This makes the codes inefficient and difficult to read. In VEGA2.0, this problematic data structure is reorganized through classifying the variables by their characteristics and grouping the variables for easier communication.

Another change through the reconstruction is that the system layout has been established as shown in Fig. 2. In the former VEGA, only the “Read input files” and “Mesh Generation” parts existed in the middle of this layout. However, in VEGA2.0, the parts that prepare to receive the input files and create the output grid files are added. Through these parts, connectivity with other codes can be ensured, and analysis of meshes is facilitated through input/output data.

B. Modification for flexibility

To generate the grid robustly, VEGA2.0 modified many functions in the reconstruction process. The first one is a modification of the constraint during the grid generation. VEGA expands the grid from the separatrix lines through the normal vector tracing method [7]. In this expansion, especially near the boundary of each section such as X-point or divertor plate, some grid points are twisted due to the narrow-angle. In former VEGA, a constraint is employed to move the problematic point to near the adjacent point. This way of constraint can cause the local expansion/compression of the grid cell which can cause the local numerical error and contaminates the whole area in the plasma solver using Finite Volume Method (FVM). Therefore, in VEGA2.0, the constraint is modified to minimize the grid distortion. As shown in Fig. 3, if the grid point twisted near the boundary of a section, the new normal vector is calculated from the following equations.

\[ V_{\text{new}} = (1 - w)V_{\text{old}} + w \cdot V_{\text{boundary}} \] (1)

\[ w = \frac{1}{2} \left( 1 + \text{erf} \left( N_e - P_i \right) \right) \] (2)
Where $V_{\text{new}}, V_{\text{old}}, V_{\text{boundary}}$ are the direction vectors as shown in Fig. 3 and $w$ is a weighting factor which consists of the error function as shown in the equation where $N_c$ and $P_i$ are the control and the position number respectively. New grid points are generated following the modified normal vector $V_{\text{new}}$ which is a combination of the original normal vector, $V_{\text{old}}$ and the boundary vector, $V_{\text{boundary}}$. Controlling the number of $N_c$ would make $w$ diminished rapidly away from the boundary vector.

The next modification is an improvement of the first point finding algorithm. VEGA uses the vector-following method to generate the contour lines of the magnetic field from the X-point. However, near the X-point, since the magnetic field hardly changes from zero, the accuracy of the direction vector is not guaranteed. Therefore, the first points of the separatrix line from the X-point are taken from the first point finding algorithm by the linear interpolation in the searching area [7].

But the searching area is only 4 cells and the number of the first point are also limited as 4 in VEGA. These restricted conditions are able to cause the high numerical error or lose the scalability to the other magnetic configurations. So in VEGA2.0, the searching area is expanded to 9 cells and the available first points are increased up to 12 as shown in Fig. 4.

Through these two major modifications, VEGA2.0 can generate grid flexible in the various magnetic configurations.

2. Bridge code

Since its development, the grid of the former VEGA has never been used to simulate the plasma transport coupled with C2. It is because the format of the grid produced by VEGA differs from that of C2. Therefore, the bridge code is newly developed to match the grid formats of the two codes, to divide the input files according to the Message Passing Interface (MPI) [10] used in C2, and to generate data other than the grid information.

A. Matching the Grid Format

VEGA2.0 is designed to store the grid of the entire tokamak plasma region in one matrix based on the separatrix lines, as shown in Fig. 5 (a). Therefore, in order to convert the grid data in this matrix into a grid format accepted by C2, the matrix should be split according to each separatrix line, which is separated by an X-point. By combining this separated grid matrix parts, the input grid files are generated according to the order of grid data and domain classification based on the direction of the magnetic field as shown in Fig. 5 (b). This domain classification is partitioned according to the computational domain of processors assigned through MPI.

![Fig. 3. Schematic cartoon of a computational domain with a separatrix line and several boundary vectors associated with X-points and divertor plates.](image)

![Fig. 4. Schematic view of grid points around the X-point with dotted separatrix lines. As an example, the first points are marked with red circles on the searching area.](image)

![Fig. 5. Schematic diagram of grid format. a) Output grid format of VEGA2.0 and b) the order and format of the grid input in C2.](image)
Table 2. The variables and their definition of 1-D data for core input file in C2

<table>
<thead>
<tr>
<th>Variables</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>rho</td>
<td>Effective minor radius $\frac{\rho}{\sqrt{n_0}}$</td>
</tr>
<tr>
<td>a meter</td>
<td>Minor radius</td>
</tr>
<tr>
<td>shift</td>
<td>Shafranov shift</td>
</tr>
<tr>
<td>elong</td>
<td>Elongation</td>
</tr>
<tr>
<td>tri</td>
<td>Triangularity</td>
</tr>
<tr>
<td>rtor</td>
<td>Major radius</td>
</tr>
<tr>
<td>g11</td>
<td>Metric coefficient $g_{11} = V' \frac{\partial \rho}{\partial \rho}$ $\approx \frac{2 \pi \int b_\rho , dl}{4 \pi^2 \rho R}$</td>
</tr>
<tr>
<td>g22</td>
<td>Volume derivative $V' = \frac{\partial V}{\partial \rho} \approx 4 \pi^2 \rho R$</td>
</tr>
<tr>
<td>g33</td>
<td>FLux surface quantity $B_\rho R$</td>
</tr>
</tbody>
</table>

B. Adding Other Data

For completion of input files for C2, other information that C2 needs must be included. In these data, a poloidal and a toroidal magnetic field, and inter-domain matching conditions for communicating the boundary data of each computational domain through MPI are included. For the case of core input file, a 1-D special information is added to calculate the magnetic surface averaged current profile and heat and momentum diffusivities.

The magnetic field value is calculated from the given plasma equilibrium data and assigned to each grid point. The inter-domain matching condition is the information required when the computation domain assigned to each processor through MPI exchanges data at its boundary. Therefore, the exact number and order of what a grid point can meet the grid point in the other computation domain. The last item, 1-D spatial information, is only for the core grid input file. This is shown in Table 2. The minor and the major radius, the effective minor radius which is defined on the magnetic flux surface, the plasma shape variables, and coordinate-related information are the components of this 1-D data. Most of these variables are an averaged value along the magnetic flux surface at the grid position of the 2-D core.

III. RESULTS

In this chapter, two kinds of results are presented. The first one shows the grid data provided from both former VEGA and VEGA2.0 to verify the upgrade of the mesh generator. In this process, a comparative analysis is performed quantitatively using the mesh quality factor used to verify the former VEGA. The second is to verify that the VEGA2.0 and C2 are well connected through the developed bridge code, and then perform a plasma simulation using this 2-D core-edge coupled plasma transport modelling package.

1. Grid Generation Results for Verification of VEGA2.0

The verification of VEGA2.0 is conducted with comparing the grid results of the same plasma state, in this case of KSTAR CDN plasma, with those of the former VEGA. The input plasma equilibrium data is provided by a free boundary MHD equilibrium code, Tokamak Equilibrium Solver (TES) [11], as shown in Fig. 6. The grid distribution is set as higher near the boundary region such as X-points, the separatrix lines, and the divertor plates.

In Fig. 7, the results of both former VEGA and VEGA2.0 are presented. The both grid generation is successfully conducted and seems to fit well each other. However, the differences between the meshes near the boundary region are certainly noticeable, especially near the X-points. These differences are mainly caused by the modifications of constraint and the first point finding algorithm. To be specific, the grid cells near the X-point are nearly triangular shapes in the result of former VEGA, which can produce local grid compression. On the other hand, in the result of VEGA2.0, the orthogonality is not collapsed much since the adjacent grid points move accordingly.

Fig. 6. Contour plots of the plasma equilibrium data of KSTAR tokamak provided by the TES code.
For the more quantitatively comparative analysis, the mesh quality factors are evaluated. Based on the preference of using FVM, the mesh quality factors of ‘Cell orthogonality’, ‘Radial flux deviation’, and ‘Field alignment’ were introduced [7]. The ‘Cell orthogonality’ represents the orthogonal property of each grid cell by calculating the deviation of the degree from the right angle. The ‘Radial flux deviation’ shows the surface normal deviations in the radial direction of the real geometry. And the ‘Field alignment’ is a standard deviation between the poloidal grid contour and the magnetic flux surfaces. Here, the ‘Field alignment’, another mesh quality factor introduced in [7] is excluded because both of the codes using the same vector-following method.

The results of the two mesh quality factors are shown in Fig. 8. Each column represents the cell averaged value of each domain corresponding to the number shown in Table 3. In Fig. 8 a), the ‘Cell orthogonality’ of VEGA2.0 is a little higher than that of the former VEGA in the most of the domain. On the other hand, the values of the all domain except core show the better results of the ‘Radial flux deviation’ as shown in Fig. 8 b). These results can be inferred that the modification of the constraint caused a observable change near the boundary of each section of the grid. Also, one can say that VEGA2.0 is able to generate a better grid for the analysis of the plasma in the edge/SOL region.

2. Simulation of 2-D Plasma Transport in KSTAR

In this section, a confirmation of the coupling between C2 and VEGA2.0 through the developed bridge code and the plasma transport simulation results of the KSTAR CDN configuration by using this completed 2-D core-edge coupled modelling package are presented.

A. Confirmation of coupling between C2 and VEGA2.0

Confirming the coupling between the plasma transport solver, C2, and the upgraded mesh generator, VEGA2.0, proceeds as follows. First, when C2 takes the input grid files, it calculates the center position of each grid cell where the plasma variables stored in. Then, at the beginning of the plasma calculation, the initial plasma values set by the user are stored at this location. Therefore, by comparing 2-D profiles generated with these initial values to the input grid, it can be confirmed whether C2 receives the grid generated by VEGA2.0 well.

The results of the above procedure are shown as lower half of the poloidal plane in Fig. 9. This figure is made by aligning the location of the initial data from C2 on the grid data plot that VEGA2.0 creates. As shown, the initial plasma values are well centered in the grid cell regardless some low orthogonality near the X-point. Thus, the bridge code allows the C2 to accept the grid of VEGA2.0, and conducting the 2-D core-edge coupled plasma simulation is possible.

In addition, at the plasma boundary such as the divertor plates, outer side of SOL, and the private region, it can be seen that the transport calculations are made in the middle of the boundary lines, not the center of the cell.

Table 3. The assigned number of each computational domain.

<table>
<thead>
<tr>
<th>Outer SOL</th>
<th>Lower Private</th>
<th>Inner SOL</th>
<th>Upper Private</th>
<th>CORE</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>5</td>
</tr>
</tbody>
</table>

Fig. 7. The results of the grid for CDN configuration in KSTAR.

Fig. 8. The results of cell averaged grid quality factor for each domain of a) ‘Cell orthogonality’ and b) ‘Radial flux deviation’. The blue column is for former VEGA and the red for VEGA2.0.
B. Simulation Results of KSTAR CDN Plasma

In this section, simulation of the plasma transport is conducted through the completed 2-D core-edge coupled modelling package. The target plasma is an L-mode plasma of KSTAR in CDN configuration, and the corresponding main parameters are shown in Table 4. In this table, ‘Tolerance’, ‘Max matrix solver iteration’, and ‘Max residue’ are the controlling factors for the iterative matrix solver in C2. The plasma equilibrium data for this target is calculated from the TES code. The initial conditions for temperature and density profiles of electron and ion, as well as the boundary conditions, are set as shown in Table 5. The simulation is conducted with an ohmic heating for 3000 normalized unit time steps or about 217 microseconds in real time.

The simulation results are presented in Fig. 10. The area near the magnetic null points such as O- or X-points is excluded from the calculation because the grid diverges or converges.

The electron temperature increases from the initial condition of 1000 eV to 1586.21 eV in the core region and dropped steeply to 100 eV near the separatrix line. Also, looking closer at the divertor region, the temperature of SOL region is hardly diffused to the private region. In other words, considering the flow velocity, it can be said that most of the heat transport is convective rather than conductive in the divertor region. In the case of ion, the core temperature is 1212.32 eV, which is lower than electrons, but with a similar profile. The density of the ion increases up to about $2.94 \times 10^{19}$ from the initial condition in the core. In the case of neutrals, they are produced highly near the divertor region, especially outer region, and has a very weak influence on the core region. In Fig. 10 e), it can be seen that the flow of the plasma varies in sign depending on the position. This is because there is a direction in the flow that follows the direction of the grid. Considering this, most of the plasma is shown to flow to the divertor plates. The normalized viscosity is calculated only in the core region in this work which shows a hollow profile on the poloidal plane.

In short, plasma transport simulation of the KSTAR L-mode plasma is conducted. Although the results may vary depending on the heat and momentum transport model, the very peaked temperature profiles and the broad density profiles are obtained. Furthermore, in the region near the divertor, which is known to have a high collision rate due to the low temperature, the plasma temperature seems to be more diffused by convection than conduction.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Value (Unit)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Major radius</td>
<td>1.8 (m)</td>
</tr>
<tr>
<td>Minor radius</td>
<td>0.5 (m)</td>
</tr>
<tr>
<td>Elongation</td>
<td>1.7</td>
</tr>
<tr>
<td>Triangularity</td>
<td>0.4</td>
</tr>
<tr>
<td>Toroidal field</td>
<td>1.8 (T)</td>
</tr>
<tr>
<td>Plasma current</td>
<td>600 (kA)</td>
</tr>
<tr>
<td>$Z$ effect</td>
<td>2</td>
</tr>
<tr>
<td>Tolerance</td>
<td>$10^{-3}$, neutral $10^{-7}$, others</td>
</tr>
<tr>
<td>Max matrix solver iteration</td>
<td>100</td>
</tr>
<tr>
<td>Max residue</td>
<td>$10^{-12}$</td>
</tr>
</tbody>
</table>

Table 4. Main operation parameters for the KSTAR L-mode plasmas.

<table>
<thead>
<tr>
<th>Initial Density ($\times 10^{19}$)</th>
<th>CORE</th>
<th>Separatrix</th>
<th>Wall</th>
</tr>
</thead>
<tbody>
<tr>
<td>Initial Temp. (eV)</td>
<td>$1.0 \times 10^3$</td>
<td>$10^2$</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Table 5. The initial condition of plasma density and temperature for both electron and ion at the magnetic center, separatrix line, and wall. The red circled parameters indicate the boundary conditions.
IV. CONCLUSIONS

The 2-D core-edge coupled plasma modelling package for analysis of tokamak transport is completed by upgrading the mesh generator, VEGA to VEGA2.0, and by developing a bridge code to couple this VEGA2.0 to the 2-D plasma transport solver, C2. The upgrade of the grid generator is conducted with the reconstruction, translation of the programming language from MATLAB to C++, and modification of the internal functions, the constraint for twisted mesh and the first point finding algorithm. The bridge code is developed so that the output grid of VEGA2.0 is converted into the input grid files of C2. The upgrade mesh generator is verified by comparing the output grid with that of former VEGA with the grid quality factors. The coupling by the bridge code is evaluated by comparing the VEGA2.0 grid with the initial profile produced by C2. The both results show that the 2-D core-edge coupled modelling code is successfully completed. Therefore, with this package, first coupled plasma transport simulation is carried out for the KSTAR L-mode plasmas in CDN configuration.

In the future, this package will be improved to observe plasma profiles and divertor heat flux changes depending on the various magnetic field configurations. The candidates of this include a Disconnected Double Null (DDN) or biased double null configuration in which the two X-points are broken in the Double Null (DN) geometry, or a snowflake or super X divertor configuration designed to dissipate the divertor heat flux. As the coupled modelling package has limitations on dynamic plasma simulations yet, it will be upgraded to deal with the time-evolving plasmas.

REFERENCES


